

restated here:

$$(3.99) \quad \bar{\Sigma}_t = G_t \Sigma_{t-1} G_t^T + R_t$$

$$(3.100) \quad \bar{\mu}_t = g(u_t, \mu_{t-1})$$

Substituting  $\Sigma_{t-1}$  by  $\Omega_{t-1}^{-1}$  and  $\bar{\mu}_t$  by  $\bar{\Omega}_t^{-1} \bar{\xi}_t$  gives us the prediction equations of the extended information filter:

$$(3.101) \quad \bar{\Omega}_t = (G_t \Omega_{t-1}^{-1} G_t^T + R_t)^{-1}$$

$$(3.102) \quad \bar{\xi}_t = \bar{\Omega}_t g(u_t, \Omega_{t-1}^{-1} \xi_{t-1})$$

The measurement update is derived from Equations (3.60) and (3.61). In particular, (3.61) defines the following Gaussian posterior:

$$(3.103) \quad \text{bel}(x_t) = \eta \exp \left\{ -\frac{1}{2} (z_t - h(\bar{\mu}_t) - H_t (x_t - \bar{\mu}_t))^T Q_t^{-1} (z_t - h(\bar{\mu}_t) - H_t (x_t - \bar{\mu}_t)) - \frac{1}{2} (x_t - \bar{\mu}_t)^T \bar{\Sigma}_t^{-1} (x_t - \bar{\mu}_t) \right\}$$

Multiplying out the exponent and reordering the terms gives us the following expression for the posterior:

$$(3.104) \quad \begin{aligned} \text{bel}(x_t) &= \eta \exp \left\{ -\frac{1}{2} x_t^T H_t^T Q_t^{-1} H_t x_t + x_t^T H_t^T Q_t^{-1} [z_t - h(\bar{\mu}_t) + H_t \bar{\mu}_t] \right. \\ &\quad \left. - \frac{1}{2} x_t^T \bar{\Sigma}_t^{-1} x_t + x_t^T \bar{\Sigma}_t^{-1} \bar{\mu}_t \right\} \\ &= \eta \exp \left\{ -\frac{1}{2} x_t^T [H_t^T Q_t^{-1} H_t + \bar{\Sigma}_t^{-1}] x_t \right. \\ &\quad \left. + x_t^T [H_t^T Q_t^{-1} [z_t - h(\bar{\mu}_t) + H_t \bar{\mu}_t] + \bar{\Sigma}_t^{-1} \bar{\mu}_t] \right\} \end{aligned}$$

With  $\bar{\Sigma}_t^{-1} = \bar{\Omega}_t$  this expression resolves to the following information form:

$$(3.105) \quad \text{bel}(x_t) = \eta \exp \left\{ -\frac{1}{2} x_t^T [H_t^T Q_t^{-1} H_t + \bar{\Omega}_t] x_t + x_t^T [H_t^T Q_t^{-1} [z_t - h(\bar{\mu}_t) + H_t \bar{\mu}_t] + \bar{\xi}_t] \right\}$$

We can now read off the measurement update equations by collecting the terms in the squared brackets:

$$(3.106) \quad \Omega_t = \bar{\Omega}_t + H_t^T Q_t^{-1} H_t$$

$$(3.107) \quad \xi_t = \bar{\xi}_t + H_t^T Q_t^{-1} [z_t - h(\bar{\mu}_t) + H_t \bar{\mu}_t]$$

### 3.5.6 Practical Considerations

When applied to robotics problems, the information filter possesses several advantages over the Kalman filter. For example, representing global uncertainty is simple in the information filter: simply set  $\Omega = 0$ . When using moments, such global uncertainty amounts to a covariance of infinite